

1st January



Corbettmaths

Prove  $(2n + 2)^2 - (2n + 1)$  is always odd.

$$\begin{aligned}
 &= (2n+2)(2n+2) - (2n+1) \\
 &= 4n^2 + 8n + 4 - 2n - 1 \\
 &= 4n^2 + 6n + 3 \\
 &= 4n^2 + 6n + 2 + 1 \\
 &= 2(2n^2 + 3n + 1) + 1
 \end{aligned}$$

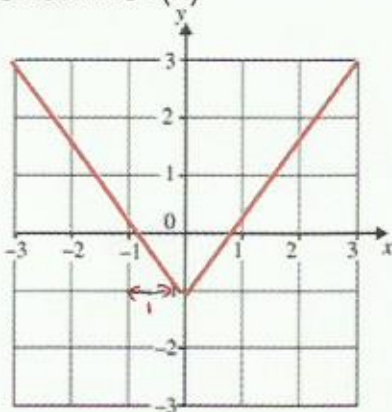
even + 1 = odd

Rationalise the denominator

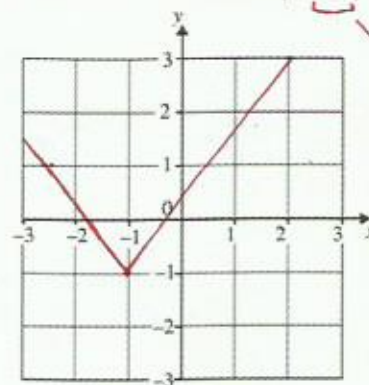
$$\frac{3 + \sqrt{2}}{\sqrt{3}}$$

$$\begin{aligned}
 &= \frac{\sqrt{3}(3 + \sqrt{2})}{\sqrt{3}\sqrt{3}} \\
 &= \frac{3\sqrt{3} + \sqrt{6}}{3} \\
 &= \sqrt{3} + \frac{\sqrt{6}}{3}
 \end{aligned}$$

Shown is  $f(x)$



Sketch the function  $f(x + 1)$



shift 1 unit left (translate)

$$f(x) = 3x + 2$$

$$g(x) = x^2$$

$$\begin{aligned}
 \text{Find } fg(x) &= f(x^2) \\
 &= 3x^2 + 2
 \end{aligned}$$

$$\text{Find } gf(5) = g(3x + 2)$$

$$= (3x + 2)^2$$

$$x = 5 \rightarrow = 17^2$$

$$= 289$$