

3rd January



Corbettmaths

$$25^{-0.5}$$

$$= \frac{1}{25^{0.5}}$$

$$= \frac{1}{\sqrt{25}} = \frac{1}{5}$$

Prove

$$(n+1)^2 - (n-1)^2 + 4$$

is always even, if  $n$  is a positive integer.

$$= n^2 + 2n + 1 - (n^2 - 2n + 1) + 4$$

$$= n^2 + 2n + 1 - n^2 + 2n - 1 + 4$$

$$= 4n + 4$$

$$= 4(n+1) \therefore \text{Multiple of 4}$$

$$\therefore \text{Even if } n > 0 \text{ and integer}$$

Rationalise the denominator

$$\frac{\sqrt{3}}{\sqrt{2}}$$

$$\frac{\sqrt{3}}{\sqrt{2}} = \frac{\sqrt{2}}{\sqrt{2}} \left( \frac{\sqrt{3}}{\sqrt{2}} \right)$$

$$= \frac{\sqrt{6}}{2}$$

Find the equation of the line that is perpendicular to  $3x + y = 8$  and passes through the point  $(1, 5)$

$$3x + y = 8$$

$$y = 8 - 3x$$

$$\text{Gradient} = -3$$

Perpendicular line:  $m = \frac{-1}{-3} = \frac{1}{3}$

$$\hookrightarrow y = \frac{1}{3}x + c$$

$$\text{at } (1, 5) \quad 5 = \frac{1}{3} + c \rightarrow c = \frac{14}{3}$$

$$\therefore y = \frac{1}{3}x + \frac{14}{3} \rightarrow 3y = x + 14$$

Simplify

$$(81x^8)^{-\frac{3}{4}} = \frac{1}{(81x^8)^{\frac{3}{4}}}$$

$$\rightarrow \frac{1}{(\sqrt[4]{81x^8})^3}$$

$$= \frac{1}{(3x^2)^3} = \frac{1}{27x^6}$$