

March 28th

A tank can be filled by three pipes.
Pipe A can fill the tank in 16 hours.
Pipe B can fill the tank in 12 hours.
Pipe C can fill the tank in 8 hours.

How long will it take to fill the tank when all three pipes are turned on but at the same time it is being drained by a pipe that can empty it in 6 hours?

If the tank has volume V

Pipe A fills at a rate of $V/16$

Pipe B fills at a rate of $V/12$

Pipe C fills at rate of $V/8$

Drain empties at a rate of $V/6$

Therefore net rate =

$$\frac{V}{16} + \frac{V}{12} + \frac{V}{8} - \frac{V}{6} = \frac{5V}{48}$$

Time = Volume \div rate

$$\text{Therefore time} = V \div \frac{5V}{48} = 9.6 \text{ hours} = \mathbf{9 \text{ hours } 36 \text{ minutes}}$$