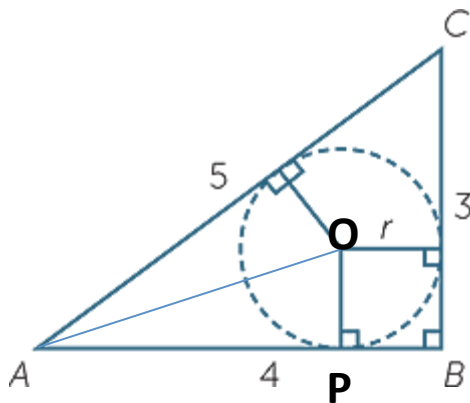


August 12<sup>th</sup>

What is the radius of the inscribed circle of a 3,4,5 right-angled triangle?



In triangle ABC

$$\tan(\angle ABC) = \frac{3}{4}$$

$$\text{Hence angle } \angle ABC = \tan^{-1} 0.75$$

$$\text{By symmetry, angle } \angle OAP = \frac{1}{2} \tan^{-1} 0.75$$

$$\text{But in triangle OAP, } \tan \angle OAP = \frac{r}{4-r}$$

$$\tan \angle OAP = \tan\left(\frac{1}{2} \tan^{-1} 0.75\right) = \frac{1}{3}$$

Hence

$$\frac{r}{4-r} = \frac{1}{3}$$

$$3r = 4 - r$$

Hence the **radius is 1**