

July 26th

$$f(x) = x^3 + 1 \quad g(x) = 3x^2 \quad h(x) = x + 3$$

If $fff(y) = 389017001$, find $gh(y)$

To find y , apply the inverse function $f^{-1}(x)$ to 389,017,001

That is, "subtract 1 and cube root"

$$389017001 - 1 = 389017000 \quad \text{cube root of } 389017000 = 730$$

$$730 - 1 = 729 \quad \text{cube root of } 729 = 9$$

$$9 - 1 = 8 \quad \text{cube root of } 8 = 2$$

Hence $y=2$

$$h(2) = 2 + 3 = 5$$

$$g(5) = 3 \times 5^2 = \mathbf{75}$$