

November 11th

If

$$ax = by = cz = 5 \quad \text{and} \quad \frac{1}{x} + \frac{1}{y} + \frac{1}{z} = 4$$

What is $a + b + c$?



If $ax = 5$ then

$$x = \frac{5}{a}$$

$$\frac{1}{x} = \frac{a}{5}$$

and similarly

$$\frac{1}{y} = \frac{b}{5} \quad \text{and} \quad \frac{1}{z} = \frac{c}{5}$$

$$\text{Hence } \frac{a}{5} + \frac{b}{5} + \frac{c}{5} = 4$$

Giving

$$\mathbf{a + b + c = 20}$$