



Prove $(2n + 2)^2 - (2n + 1)$ is always odd for all positive values of n .

$$\begin{aligned} & (2n+2)(2n+2) - (2n+1) \\ &= 4n^2 + 8n + 4 - 2n - 1 \\ &= 4n^2 + 6n + 3 \\ &= 4n^2 + 6n + 2 + 1 \end{aligned}$$

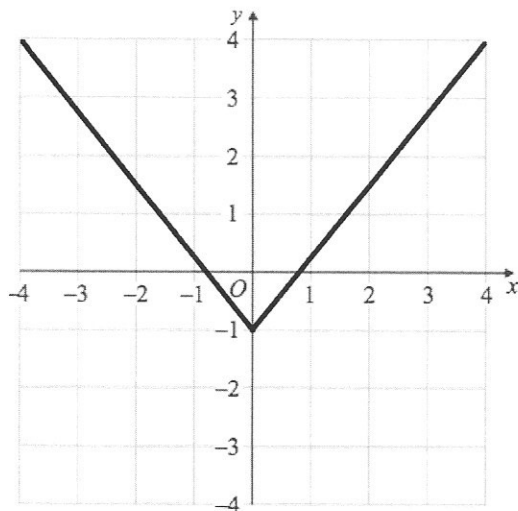
$$\begin{aligned} & 2(2n^2 + 3n + 1) + 1 \\ & \text{even} + 1 = \text{odd} \end{aligned}$$

Rationalise the denominator

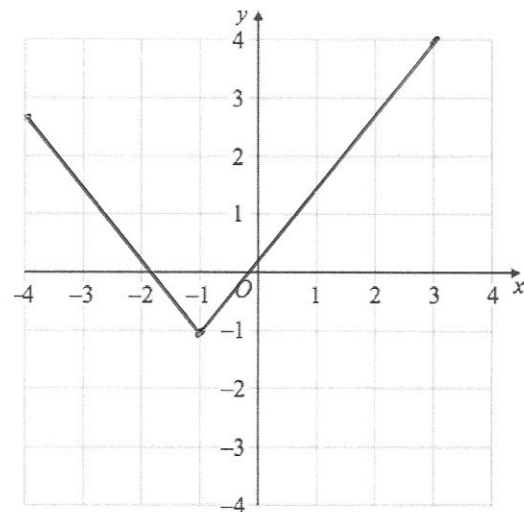
$$\frac{3 + \sqrt{2}}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} = \frac{3\sqrt{3} + \sqrt{6}}{3}$$

$$\sqrt{3} + \frac{\sqrt{6}}{3}$$

Shown is $f(x)$



Sketch the function $f(x + 1)$
left



$$f(x) = 3x + 2$$

$$g(x) = x^2$$

$$g(x) = x^2$$

$$f(x^2)$$

Find $fg(x)$

$$= 3x^2 + 2$$

Find $gf(5)$

$$f(5) = 17$$

$$g(17) = 289$$