

23rd February

CorbettmOths

Work out

$$\frac{9}{4x^3} + \frac{5}{3x} - x^2 \quad \frac{27}{12x^3} + \frac{20x^2}{12x^3} - \frac{12x^5}{12x^3}$$

$$\frac{27 + 20x^2 - 12x^5}{12x^3}$$

Give your answer as a single fraction in its simplest form

Solve the simultaneous equations

$$(1) - x - y + 3z = 5 \rightarrow \times (2)$$

$$(2) - x + y + 6z = 12$$

$$(3) - 3x - 2y + 2z = 10 \quad \times 3$$

$$2x - 2y + 6z = 10 \quad - (4)$$

$$9x - 6y + 6z = 30 \quad - (5)$$

$$x + y + 6z = 12 \quad - (2)$$

$$(5) - (2) \quad 8x - 7y = 18 \quad - (6)$$

$$(5) - (4) \quad 7x - 4y = 20 \quad - (7)$$

$$4 \times (6) \text{ and } 7 \times (7)$$

$$32x - 28y = 72 \quad - (8)$$

$$49x - 28y = 140 \quad - (9)$$

$$(9) - (8) =$$

$$17x = 68$$

$$\boxed{x = 4}$$

sub into (8)

$$128 - 28y = 72$$

$$-28y = -56$$

$$\boxed{y = 2}$$

$$\boxed{z = 1}$$

$$y = x^4 - 2x^2$$

Work out the value of $\frac{d^2y}{dx^2}$ when $x = -5$

$$\frac{dy}{dx} = 4x^3 - 4x$$

$$\frac{d^2y}{dx^2} = 12x^2 - 4$$

$$\text{when } x = -5, \frac{d^2y}{dx^2} = 296$$

Prove $n^3 - n$ is always divisible by 6. n is an integer greater than 1.

$$n^3 - n = (n-1)n(n+1)$$

Three consecutive integers

At least one number is even and one is a multiple of 3.

$$2 \times 3 = 6$$

$\therefore n^3 - n$ is always divisible by 6.