

26th April



Expand and simplify

$$(1 + 2\sqrt{3})^3$$

$$(1 + 2\sqrt{3})(1 + 2\sqrt{3})$$

$$1 + 4\sqrt{3} + 12 = (13 + 4\sqrt{3})$$

$$(1 + 2\sqrt{3})(13 + 4\sqrt{3})$$

$$13 + 4\sqrt{3} + 26\sqrt{3} + 24$$

$$\boxed{37 + 30\sqrt{3}}$$

$(x + 1)$ is a factor of
 $x^3 - 2x^2 + 3x + a$

Work out the value of a

$$f(x) = x^3 - 2x^2 + 3x + a$$

$$f(-1) = 0$$

$$-1 - 2 - 3 + a = 0$$

$$-6 + a = 0$$

$$a = 6$$

$$3^x = 9\sqrt{3} \quad \text{and} \quad 3^y = \frac{1}{\sqrt{3}}$$

Work out 3^{x-y}

$$3^x = 3^2 \times 3^{0.5} \quad x = 2.5$$

$$= 3^{2.5}$$

$$3^y = 3^{-0.5} \quad y = -0.5$$

$$3^{2.5 - (-0.5)}$$

$$3^3 = 27$$

For what values of x is
 $y = -x^2 - 7x + 12$ an increasing
 function?

$$\frac{dy}{dx} = -2x - 7$$

$$-2x - 7 > 0$$

$$-2x > 7$$

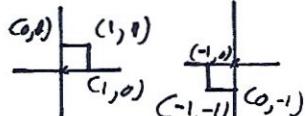
$$x < -\frac{7}{2}$$

Work out the matrix that transforms the unit square by a 180° rotation about O .

$$\begin{pmatrix} a & b \\ c & d \end{pmatrix} \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} = \begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$$

~~$b=0 \quad d=-1$~~

$$\begin{pmatrix} a & 0 \\ c & -1 \end{pmatrix} \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} = \begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix} \quad \begin{matrix} a = -1 \\ c = 0 \end{matrix}$$



$$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$$