

**31st March**

Corbettmaths

Make  $m$  the subject of  $x = \frac{8a}{k-m}$

$$kx - mx = 8a$$

$$kx - 8a = mx$$

$$m = \frac{kx - 8a}{x}$$

$$m = k - \frac{8a}{x}$$

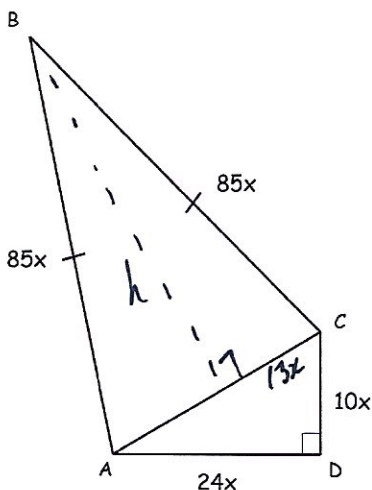
$f(x) = 10 + 3x - x^2$  for all values of  $x$

Write down the range of  $f(x)$

$$\begin{aligned} f(x) &= -(x^2 - 3x - 10) \\ &= -\left[x - \frac{3}{2}\right]^2 - \frac{9}{4} - 10 \\ &= -\left[x - \frac{3}{2}\right]^2 - \frac{49}{4} \\ &= -\left[x - \frac{3}{2}\right]^2 + \frac{49}{4} \end{aligned}$$

$$f(x) \leq \frac{49}{4}$$

Shown below is quadrilateral ABCD.  
ABC is an isosceles triangle.  
ACD is a right angled triangle.



Show that the area of quadrilateral ABCD is  $1212x^2$

$$\begin{aligned} AC^2 &= (10x)^2 + (24x)^2 \\ &= 676x^2 \end{aligned}$$

$$AC = 26x$$

$$h^2 = (85x)^2 - (13x)^2$$

$$h = 84x$$

$$\begin{aligned} \text{Area } \triangle ADC &: \frac{1}{2} \times 24x \times 10x \\ &= 120x^2 \end{aligned}$$

$$\triangle ABC: \frac{1}{2} \times 26x \times 84x = 1092x^2$$

$$1212x^2 \quad \text{QED}$$

$$y = 4x^3 + ax$$

The value of  $\frac{dy}{dx}$  when  $x = -2$  is seven

times the value of  $\frac{dy}{dx}$  when  $x = 1$

$$\frac{dy}{dx} = 12x^2 + a$$

$$\text{when } x = -2 \quad \frac{dy}{dx} = 48 + a$$

$$x = 1 \quad \frac{dy}{dx} = 12 + a$$

$$7(12 + a) = 48 + a$$

$$\boxed{a = -6}$$