

11th May



Corbettmaths

A circle, centre  $(3, -7)$  has an area of  $64\pi$

$$r = 8$$

Work out the equation of the circle.

$$(x-3)^2 + (x+7)^2 = 64$$

or

$$(x-3)^2 + (x+7)^2 = 8^2$$

The first term of a sequence is  $5 - 2a$

$$1^{\text{st}}: 5 - 2a$$

The term-to-term rule of the sequence is subtract  $4a$  and then multiply by 2

$$2^{\text{nd}}: 10 - 12a$$

$$3^{\text{rd}}: 20 - 32a$$

The fourth term of the sequence is 58

$$4^{\text{th}}: 40 - 72a$$

Work out the second term of the sequence.

$$40 - 72a = 58$$

$$-18 = 72a$$

$$a = -\frac{1}{4}$$

$$10 - 12\left(-\frac{1}{4}\right) = \boxed{13}$$

Solve the equation

$$\frac{3}{2x-1} = 1 + \frac{4}{3x-1}$$

$$\frac{3}{2x-1} - \frac{4}{3x-1} = 1$$

$$\frac{9x-3-4(2x-1)}{(2x-1)(3x-1)} = 1 \quad \left. \begin{array}{l} 6x^2 - 6x = 0 \\ 6x(x-1) = 0 \\ x=0 \text{ or } x=1 \end{array} \right\}$$

$$\frac{9x-3-8x+4}{(2x-1)(3x-1)} = 1$$

$$x+1 = 6x^2 - 5x + 1$$

Work out the equation of the normal to the curve  $y = x^3 + 2x - 5$  at the point where  $x = -2$   $y = -8 - 4 - 5 = -17$

$$\frac{dy}{dx} = 3x^2 + 2$$

$$\frac{dy}{dx} = 14$$

$$y = -\frac{1}{14}x + c$$

$$-17 = \frac{1}{7} + c$$

$$c = -\frac{120}{7}$$

$$\boxed{y = -\frac{1}{14}x - \frac{120}{7}}$$

$$y = \frac{1}{14}x - \frac{120}{7}$$