

30th November



Corbettmaths

Expand and simplify fully

$$(3-x)(x+4)^2$$

$$\begin{aligned} &(3-x)(x^2+8x+16) \\ &= 3x^2+24x+48-x^3-8x^2-16x \\ &= \underline{-x^3-5x^2+8x+48} \end{aligned}$$

$$y = \frac{4}{x^2}$$

Find  $\frac{dy}{dx}$ 

$$\begin{aligned} y &= 4x^{-2} \\ \Rightarrow \frac{dy}{dx} &= -8x^{-3} = \underline{-\frac{8}{x^3}} \end{aligned}$$

Show that

$$(\sin\theta + \cos\theta)^2 + (\sin\theta - \cos\theta)^2 \equiv 2$$

$$\begin{aligned} \text{LHS} &= \sin^2\theta + 2\sin\theta\cos\theta + \cos^2\theta \\ &\quad + \sin^2\theta - 2\sin\theta\cos\theta + \cos^2\theta \\ &= 2(\sin^2\theta + \cos^2\theta) \\ &= \underline{2} \end{aligned}$$

The unit square is transformed by matrix **Q** followed by matrix **R** followed by the matrix **S**

This is equivalent to transforming the unit square by the identity matrix.

Matrix **R** represents a rotation.  
Matrices **Q** and **S** represent reflections.

Write down three possible matrices for **Q**, **R** and **S**

E.g. **R** rotation  $180^\circ$  abt  $(0,0)$   
**Q** reflection in  $y$ -axis  
**S** reflection in  $x$ -axis

$$\underline{\underline{R}} = \begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$$

$$\underline{\underline{Q}} = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$$

$$\underline{\underline{S}} = \begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$$