

Name: _____

Exam Style Questions

Geometric Progressions



Equipment needed: Pen and Calculator

Guidance

1. Read each question carefully before you begin answering it.
2. Check your answers seem right.
3. Always show your workings

Video Tutorial

www.corbettmaths.com/contents

Video 375



Answers and Video Solutions



1. Here are the first five terms of a sequence



1 4 16 64 256

- (a) Work out the next term in the sequence

$$256 \times 4 = 1024$$

1024
.....
(1)

- (b) Explain how you worked out the answer to part (a).

The common ratio is 4 ($4 \div 1 = 4$, $16 \div 4 = 4$ etc)

so $256 \times 4 = 1024$.

.....
(1)

2. The first two terms of a geometric progression are 5 and 15



Work out the next term.

$$5 \xrightarrow{\times 3} 15 \xrightarrow{\times 3} 45$$

$$15 \div 5 = 3$$

$$15 \times 3$$

45
.....

(1)

3. A geometric progression begins 2, 10, ...



Work out the next three terms.

$$2 \xrightarrow{\times 5} 10 \xrightarrow{\times 5} 50 \xrightarrow{\times 5} 250 \xrightarrow{\times 5} 1250$$

50 250 1250
.....
(2)

4. Which of the following is a geometric progression?



Circle the correct answer.

$$\begin{array}{ccc} +3 & +3 & +3 \\ 5 & 8 & 11 & 14 \end{array} \quad \times$$

$$\begin{array}{ccc} 5+6=11 \\ 6+11=17 \\ 5 & 6 & 11 & 17 \end{array} \quad \times$$

$$\begin{array}{ccc} \times 2 & \times 2 & \times 2 \\ 5 & 10 & 20 & 40 \end{array} \quad \checkmark$$

$$\begin{array}{ccc} +2 & +4 & +6 \\ 5 & 7 & 11 & 17 \end{array} \quad \times$$

(1)

5. Which of the following is a geometric progression?



Circle the correct answer.

$$\begin{array}{ccc} +2 & +2 & +2 \\ 2 & 4 & 6 & 8 \end{array} \quad \times$$

$$\begin{array}{ccc} 2+3=5 \\ 3+5=8 \\ 2 & 3 & 5 & 8 \end{array} \quad \times$$

$$\begin{array}{ccc} 2 & 4 & 6 & 10 \end{array} \quad \times$$

$$\begin{array}{l} 2+4=6 \\ 6+4=10 \end{array}$$

$$\begin{array}{ccc} \times 2 & \times 2 & \times 2 \\ 2 & 4 & 8 & 16 \end{array} \quad \checkmark$$

(1)

6. The second and third terms of a geometric progression are shown.



$$\dots \xrightarrow{\times 4} 2 \xrightarrow{\times 4} 8 \xrightarrow{\times 4} 32 \dots$$

Work out the first and the fourth terms of the progression.

$$2 \div 4 = 0.5$$

First term 0.5

Fourth term 32

(2)

7. The first two terms of a geometric progression are shown.



$$60 \xrightarrow{\times \frac{1}{5}} 12 \xrightarrow{\times \frac{1}{5}} \dots$$

Work out the third term of the progression.

$$12 \times \frac{1}{5} = \frac{12}{5}$$

$$\text{or } 12 \div 5 = 2.4$$

$$\begin{array}{r} 02.4 \\ 5 \overline{)12.0} \end{array}$$

$$\dots\dots\dots 2.4 \text{ or } \frac{12}{5} \quad (1)$$

8. The first three terms of a geometric progression are shown.



$$\frac{4}{5} \xrightarrow{\times \frac{3}{7}} \frac{12}{35} \xrightarrow{\times \frac{3}{7}} \frac{36}{245}$$

Work out the fourth term of the progression.

$$\frac{12}{35} \div \frac{4}{5} = \frac{3}{7}$$

$$\frac{36}{245} \times \frac{3}{7} = \frac{108}{1715}$$

$$\text{or } \frac{36}{245} \div \frac{12}{35} = \frac{3}{7}$$

$$\dots\dots\dots \frac{108}{1715} \quad (1)$$

9. The first and third terms of a geometric progression are shown.
All the terms in the progression are positive.



$$3 \xrightarrow{\times y} \dots \xrightarrow{\times y} 48 \xrightarrow{\times 4} \dots$$

$$\quad \quad \quad 12 \quad \quad \quad 192$$

Work out the fourth term of the progression.

$$3 \times y \times y = 48$$

$$y \times y = 16$$

$$y = 4$$

$$\begin{array}{r} 48 \\ \times 4 \\ \hline 192 \end{array}$$

$$\dots\dots\dots 192 \quad (2)$$

10. The second and fourth terms of a geometric progression are shown.
All the terms in the progression are negative.



$$-\frac{2}{3} \dots -2 \xrightarrow{\times y} -6 \dots -18$$

Work out the first of the progression.

$$-2 \times y \times y = -18$$

$$y \times y = 9$$

$$y = 3$$

$$-2 \div 3 = -\frac{2}{3}$$

$$-\frac{2}{3} \dots$$

(2)

11. The first two terms of a geometric sequence are 3 and 12.




Find the sum of the first 5 terms of the geometric sequence.

$$3 \xrightarrow{\times 4} 12 \xrightarrow{\times 4} 48 \xrightarrow{\times 4} 192 \xrightarrow{\times 4} 768$$

$$3 + 12 + 48 + 192 + 768 = 1023$$

$$1023 \dots$$

(3)

12. The fifth term of a geometric sequence is 3072
 The sixth term of the geometric sequence is 24576

Find the first term of the geometric sequence.


$$24576 \div 3072 = 8$$

1 st	2 nd	3 rd	4 th	5 th	6 th
0.75	6	48	384	3072	24576

$$\frac{3}{4}$$

(3)

13. The ninth term of a geometric progression is double the tenth term.

 The first term of the geometric progression is 300

Find the third term of the geometric progression.

$$\begin{array}{ccc} 9^{\text{th}} & & 10^{\text{th}} \\ & \swarrow & \\ & \times \frac{1}{2} & \end{array}$$

$$300 \times \frac{1}{2} = 150$$

$$150 \times \frac{1}{2} = 75$$

$$75$$

(2)

14. A is an arithmetic progression.



The n th term of A is $9n - 3$

B is a geometric progression.

The first three terms of B are: 3 6 12

The 43rd term of A is the x th term of B.

Find x .

$$A: 9n - 3$$

$$9 \times 43 - 3 = 384$$

B:	1 st	2 nd	3 rd	4 th	5 th	6 th	7 th	8 th
	3	6	12	24	48	96	192	384

8

(4)

15. The second term of a geometric progression is 48



The sixth term of the same progression is 12288

Find the fifth term.

1 st	2 nd	3 rd	4 th	5 th	6 th
	48				12288
		$\times y$	$\times y$	$\times y$	$\times y$

$$12288 \div 4 = 3072$$

$$48y^4 = 12288$$

$$y^4 = 256$$

$$y = 4$$

3072

(3)

16. Here are the first four terms of a sequence.



$$2 \xrightarrow{\times \sqrt{7}} 2\sqrt{7} \xrightarrow{\times \sqrt{7}} 14 \xrightarrow{\times \sqrt{7}} 14\sqrt{7}$$

Work out the fifth term of the sequence.

$$14\sqrt{7} \times \sqrt{7}$$

$$= 14\sqrt{49}$$

$$= 14 \times 7$$

$$= 98$$

98

(2)

17. Here are the first three terms of a sequence.



$$6\sqrt{3} \xrightarrow{\times \sqrt{3}} 18 \xrightarrow{\times \sqrt{3}} 18\sqrt{3}$$

Work out the fourth term of the sequence.

$$18\sqrt{3} \times \sqrt{3}$$

$$= 18\sqrt{9}$$

$$= 18 \times 3$$

$$= 54$$

54

(2)

18. Here are the first four terms of a sequence.



$$\sqrt{3} \quad 6 \xrightarrow{\times 2\sqrt{3}} 12\sqrt{3} \quad 72 \xrightarrow{\times 2\sqrt{3}}$$

Work out the next term of the sequence.

$$12\sqrt{3} \div 6 = 2\sqrt{3}$$

$$72 \times 2\sqrt{3} = 144\sqrt{3}$$

$$144\sqrt{3}$$

(2)

19. S is a geometric sequence.



The first three terms of S are $(x - 15)$, x and $(3x + 20)$, where x is positive.

Find the value of x .

$$\frac{x}{x-15} \neq \frac{3x+20}{x}$$

$$x^2 = (3x + 20)(x - 15)$$

$$x^2 = 3x^2 - 45x + 20x - 300$$

$$0 = 2x^2 - 25x - 300$$

$$0 = (2x + 15)(x - 20)$$

$$x = -\frac{15}{2} \text{ or } x = 20$$

$$20$$

(5)

20. S is a geometric sequence.



The first three terms of S are $(x + 18)$, x and $(2x - 15)$, where x is positive.

Find the value of x .

$$\frac{x}{x+18} \neq \frac{2x-15}{x}$$

$$x^2 = (2x - 15)(x + 18)$$

$$x^2 = 2x^2 + 36x - 15x - 270$$

$$0 = x^2 + 21x - 270$$

$$0 = (x + 30)(x - 9)$$

$$x = -30 \quad x = 9$$

x

9

(5)