

Name:

Exam Style Questions

## Sequences: nth term



Corbettmaths

Equipment needed: Pen and Calculator

### Guidance

1. Read each question carefully before you begin answering it.
2. Check your answers seem right.
3. Always show your workings

Video Tutorial

[www.corbettmaths.com/contents](http://www.corbettmaths.com/contents)

Video 288



Answers and Video Solutions



1. Here are the first five terms in a number sequence.

7 10 13 16 19 22 25 28 31 34

- (a) Find the 10th term in this number sequence.

34

(2)

- (b) Write an expression, in terms of  $n$ , for the  $n$ th term of this number sequence.

7 10 13 16

3n 3 6 9 12

$3n + 4$

(2)

2. A number sequence has  $n$ th term of  $6n + 3$

- (a) Write down the first four terms of this sequence.

1st term 9, 2nd term 15, 3rd term 21, 4th term 27

(3)

- (b) Sara says that 1008 is a term in this sequence.

Explain why she is wrong.

1008 is even, but all terms in the sequence  $6n + 3$  will be odd.

(1)

3. A sequence of numbers is shown below.

1      5      9      13      17      ...      ...

- (a) Find an expression for the  $n$ th term of the sequence.

1      5      9      13  
 $4n$     4    8    12    16

$$\frac{4n-3}{(2)}$$

- (b) Explain why 95 will not be a term in this sequence.

$$4n - 3 = 95$$

$$4n = 98$$

$$n = 24.5$$

95 is between the 24th and 25th terms.  
 .....  
 .....  
 (2)

4. The  $n$ th term of a number sequence is given by  $5n + 2$

- (a) Work out the first three terms of the number sequence.

1st term ..... 7, 2nd term ..... 12, 3rd term ..... 17  
 (2)

Here are the first five terms of another number sequence.

5      11      17      23      29

- (b) Find, in terms of  $n$ , an expression for the  $n$ th term of this sequence.

5      11      17      23  
 $6n$     6      12    18    24

$$\frac{6n-1}{(2)}$$

5. A sequence of numbers is shown.

2    9    16    23    30    ...    ...

- (a) Find an expression for the  $n$ th term of the sequence.

2    9    16    23  
7    14    21    28

$$\frac{7n - 5}{(2)}$$

- (b) Find the 100th term in the sequence.

$$7 \times 100 - 5$$

$$\frac{695}{(2)}$$

6. Here is the linear sequence

10    16    22    28  
 $6n$     6    12    18    24

Circle the  $n$ th term of the sequence

$$4n + 6$$

$$n + 6$$

$$6n + 4$$

$$6n$$

(2)

7. The  $n$ th term of a number sequence is  $n^2 + 3$

(a) Find the first three terms of this sequence.

1st term .....4....., 2nd term .....7....., 3rd term .....12.....  
(2)

(b) Work out the difference between the 5th and 10th terms in the sequence.

$$\begin{array}{l} \text{5th term} \\ \hline 5^2 + 3 \\ 25 + 3 = 28 \end{array}$$

$$\begin{array}{l} \text{10th term} \\ \hline 10^2 + 3 = 103 \end{array}$$

$$103 - 28 = 75$$

.....75.....  
(3)

8. The first 5 terms in a number sequence are

$-3n$       10   7   4   1   -2   ...   ...  
-3   -6   -9   -12

(a) Work out the  $n$ th term of the sequence.

$$\begin{array}{l} 13 - 3n \\ \text{or} \\ -3n + 13 \end{array}$$

.....  
(2)

(b) Find the 50th term of the sequence.

$$\begin{array}{l} 13 - 3 \times 50 \\ 13 - 150 = -137 \end{array}$$

.....-137.....  
(2)

9. Work out the  $n$ th term for this sequence

12   22   32   42   52   ...   ...  
 $10n$    10   20   30   40   .

$$\frac{10n+2}{(2)}$$

10. The  $n$ th term of a sequence is  $3n - 2$

(a) Write down the first two terms of this sequence.

1st term .....1....., 2nd term .....4.....  
(2)

(b) Which term of the sequence is equal to 70?

$$\begin{aligned} 3n - 2 &= 70 \\ 3n &= 72 \\ n &= 24 \end{aligned}$$

$$\frac{24^{\text{th}}}{(2)}$$

(c) Explain why 101 is not a term in the sequence.

$$\begin{aligned} 3n - 2 &= 101 \\ 3n &= 103 \\ n &= 34.333... \end{aligned}$$

101 will be between the  $34^{\text{th}}$  and  $35^{\text{th}}$  terms in the sequence.

(2)

11. Here are the  $n$ th terms of 4 sequences.

Sequence 1	$n$ th term	$3n + 1$
Sequence 2	$n$ th term	$5n + 10$
Sequence 3	$n$ th term	$10n$
Sequence 4	$n$ th term	$5n - 1$

For each sequence state whether the numbers in the sequence are

- A Always multiples of 5  
 S Sometimes multiples of 5  
 N Never multiples of 5

$3n + 1$	4	7	10	13	16
$5n + 10$	15	20	25	30	35
$10n$	10	20	30	40	50
$5n - 1$	4	9	14	19	24

Sequence 1 ..... S .....  
 Sequence 2 ..... A .....  
 Sequence 3 ..... A .....  
 Sequence 4 ..... N .....

(4)



12. The first four terms of an arithmetic sequence are

$$-25 \quad -37 \quad -49 \quad -61$$

Find an expression, in terms of  $n$ , for the  $n$ th term of the sequence.

$$\begin{array}{cccccc} & -25 & -37 & -49 & -61 & \\ -12n & -12 & -24 & -36 & -48 & \end{array}$$

$$\frac{-12n - 13}{(2)}$$

13. The  $n$ th term of a sequence is  $5 - 3n$

Write down the first three terms of the sequence.

$$\begin{array}{l} 5 - 3 \times 1 \\ 5 - 3 = 2 \end{array}$$

$$\begin{array}{l} 5 - 3 \times 2 \\ 5 - 6 = -1 \end{array}$$

$$\begin{array}{l} 5 - 3 \times 3 \\ 5 - 9 = -4 \end{array}$$

$$\begin{array}{l} 2 \quad -1 \quad -4 \\ \text{1st term } \dots\dots\dots, \text{ 2nd term } \dots\dots\dots, \text{ 3rd term } \dots\dots\dots \end{array}$$

(2)



14. The  $n$ th term of a sequence is  $4n - 7$

(a) Write down the first three terms of the sequence.

1st term  $-3$ , 2nd term  $1$ , 3rd term  $5$   
(2)

(b) What is the difference between the 150th and 151st terms?

4

$4$   
(1)

The last term of this sequence is 393

(c) How many terms are there in this sequence?

$$\begin{array}{r} 4n - 7 = 393 \\ + 7 \quad + 7 \\ \hline 4n = 400 \\ n = 100 \end{array}$$

$100$   
(2)

15. Find the  $n$ th term of the sequences

(a) 1, 4, 9, 16, 25, ...

$$\frac{n^2}{(1)}$$

(b) 3, 6, 11, 18, 27, ...

$$\frac{n^2 + 2}{(1)}$$

(c) -3, 0, 5, 12, 21, ...

$$\frac{n^2 - 4}{(1)}$$

(d) 2, 8, 18, 32, 50, ...

$$\frac{2n^2}{(1)}$$

16. The  $n$ th term of a sequence is  $9n + 7$

Write down all the numbers from the sequence that are **prime** and **less than 100**.

16    25    34    43    52    61    70    79    88  
97

43, 61, 79, 97

(2)

17. The first 5 terms in a number sequence are

30    25    20    15    10    ...    ...

Work out the  $n$ th term of the sequence.

$$-5n \quad -5 \quad -10 \quad -15 \quad -20$$

$$35 - 5n$$

or

$$-5n + 35$$

(2)

18. Here are the first four terms of an arithmetic sequence

9    17    25    33

- (a) Find an expression, in terms of  $n$ , for the  $n$ th term of the sequence

$$9 \quad 17 \quad 25 \quad 33$$

$$8n \quad 8 \quad 16 \quad 24 \quad 32$$

$$8n + 1$$

(2)

The  $n$ th term of a difference sequence is  $20 - 3n$

- (b) Is  $-71$  a term in the sequence?

Show your working out.

$$20 - 3n = -71$$

$$20 = -71 + 3n$$

$$91 = 3n$$

$$n = 30.333 \dots$$

No

(2)

19. The first 5 terms in a number sequence are

$$\begin{array}{ccccccccc}
 & 2 & 2.5 & 3 & 3.5 & 4 & \dots & \dots \\
 0.5n & 0.5 & 1 & 1.5 & 2 & 2.5 & & 
 \end{array}$$

- (a) Work out the  $n$ th term of the sequence.

$$\begin{array}{r}
 0.5n + 1.5 \\
 \hline
 (2)
 \end{array}$$

- (b) Work out the 20th term of the sequence.

$$\begin{array}{r}
 0.5 \times 20 + 1.5 \\
 10 + 1.5
 \end{array}$$

$$\begin{array}{r}
 11.5 \\
 \hline
 (2)
 \end{array}$$

20. The 4th term of a linear sequence is 26  
The 6th terms of the same sequence is 32

Work out the  $n$ th term of the sequence.

$$\begin{array}{cccccc}
 \underline{17} & \underline{20} & \underline{23} & 26 & \underline{29} & 32
 \end{array}$$

$$\begin{array}{cccccc}
 3n & 3 & 6 & 9 & 12 & 
 \end{array}$$

$$\begin{array}{r}
 3n + 14 \\
 \hline
 (3)
 \end{array}$$

21. The first 5 terms of a sequence are

$1 \quad 5 \quad 9 \quad 13 \quad 17$   
 $4n \quad 4 \quad 8 \quad 12$   
 (a) Work out the  $n$ th term for this sequence.

$$\frac{4n - 3}{(2)}$$

The first 5 terms of a sequence are

$\frac{1}{12} \quad \frac{5}{23} \quad \frac{9}{34} \quad \frac{13}{45} \quad \frac{17}{56}$

(a) Work out the  $n$ th term for this sequence.

$12 \quad 23 \quad 34 \quad 45 \quad \dots$   
 $1n \quad 11 \quad 22 \quad 33 \quad 44$   
 $11n + 1$

$$\frac{4n - 3}{11n + 1} \dots (2)$$

22. Here are the first 4 terms of a sequence

$\frac{2}{3} \quad \frac{3}{5} \quad \frac{4}{7} \quad \frac{5}{9} \quad \frac{6}{11}$

(a) Find the next term of the sequence

$$\frac{6}{11} \dots (1)$$

(b) Find the  $n$ th term of the sequence

$2 \quad 3 \quad 4 \quad 5$   
 $n \quad 1 \quad 2 \quad 3 \quad 4$   
 $n + 1$   
 $3 \quad 5 \quad 7 \quad 9$   
 $n \quad 2 \quad 4 \quad 6 \quad 8$   
 $2n + 1$

$$\frac{n + 1}{2n + 1} \dots (1)$$

23. Here are the first 4 terms of a sequence

$$\frac{7}{8} \quad \frac{9}{11} \quad \frac{11}{14} \quad \frac{13}{17}$$

Write down the 20th term of the sequence.

$$\begin{array}{cccc}
 7 & 9 & 11 & 13 \\
 2n & 2 & 4 & 6 & 8 \\
 & 2n+5 & & & 
 \end{array}
 \quad
 \begin{array}{cccc}
 8 & 11 & 14 & 17 \\
 3n & 3 & 6 & 9 & 12 \\
 & 3n+5 & & & 
 \end{array}$$

$$\begin{array}{r}
 2n+5 \\
 \hline
 3n+5
 \end{array}
 \quad
 \begin{array}{r}
 45 \\
 \hline
 65
 \end{array}
 \quad
 \begin{array}{r}
 9 \\
 \hline
 13
 \end{array}$$

(2)

24. Martin has written the first 50 terms of the sequence with  $n$ th term  $150 - 4n$ .

Work out which term is the first negative term.

Approach 1

$$\begin{aligned}
 150 - 4 \times 30 &= 30 \\
 150 - 4 \times 35 &= 10 \\
 150 - 4 \times 37 &= 2 \\
 150 - 4 \times 38 &= -2
 \end{aligned}$$

Approach 2

$$\begin{aligned}
 150 - 4n &= 0 \\
 150 &= 4n \\
 n &= 37.5 \\
 &\underline{38^{th}}
 \end{aligned}$$

.....38th term (-2).....  
(3)

25. The first 4 terms of sequence A are

$5n$       4      9      14      19  
             5      10      15

(a) Find the  $n$ th term of sequence A.

$$\frac{5n - 1}{\dots\dots\dots} \quad (2)$$

The  $n$ th term of sequence B is  $2n + 6$

The  $n$ th terms of sequence A and sequence B are added together to give the  $n$ th term of sequence C.

Is 1000 is a term in sequence C?

$$\begin{array}{r} 5n - 1 \\ 2n + 6 \\ \hline 7n + 5 \end{array}$$

$$\begin{aligned} 7n + 5 &= 1000 \\ 7n &= 995 \\ n &= 142.142\dots \end{aligned}$$

$No$   
 $\dots\dots\dots$   
 (2)

26. The  $n$ th term of a sequence is  $(n + 1)(n + 3)$

Work out the first three terms of the sequence.

1<sup>st</sup> term       $2 \times 4 = 8$

2<sup>nd</sup> term       $3 \times 5 = 15$

3<sup>rd</sup> term       $4 \times 6 = 24$

1st term  $8$ , 2nd term  $15$ , 3rd term  $24$   
 $\dots\dots\dots$   
 (2)