

Name: _____

Exam Style Questions

Sequences: nth term



Corbettmaths

Equipment needed: Pen and Calculator

Guidance

1. Read each question carefully before you begin answering it.
2. Check your answers seem right.
3. Always show your workings

Video Tutorial

www.corbettmaths.com/contents



Video 288

Answers and Video Solutions



1. Here are the first five terms in a number sequence.

7 10 13 16 19 22 25 28 31 34

(a) Find the 10th term in this number sequence.

34

(2)

(b) Write an expression, in terms of n , for the n th term of this number sequence.

7 10 13 16
3n 3 6 9 12

$3n + 4$

(2)

2. A number sequence has n th term of $6n + 3$

(a) Write down the first four terms of this sequence.

1st term 9 2nd term 15 3rd term 21 4th term 27
(3)

(b) Sara says that 1008 is a term in this sequence.

Explain why she is wrong.

1008 is even, but all terms in the sequence $6n + 3$ will be odd.

(1)

3. A sequence of numbers is shown below.

$$1 \quad 5 \quad 9 \quad 13 \quad 17 \quad \dots \quad \dots$$

(a) Find an expression for the n th term of the sequence.

$$\begin{array}{cccc} 1 & 5 & 9 & 13 \\ 4n & 4 & 8 & 12 & 16 \end{array} \quad \dots \quad \dots$$

$4n - 3$
(2)

(b) Explain why 95 will not be a term in this sequence.

$$4n - 3 = 95$$

$$4n = 98$$

$$n = 24.5$$

95 is between the 24th and 25th terms.

(2)

4. The n th term of a number sequence is given by $5n + 2$

(a) Work out the first three terms of the number sequence.

$$\begin{array}{lll} \text{1st term} \dots \dots \dots & 7 & \text{2nd term} \dots \dots \dots & 12 & \text{3rd term} \dots \dots \dots & 17 \end{array}$$

(2)

Here are the first five terms of another number sequence.

$$5 \quad 11 \quad 17 \quad 23 \quad 29$$

(b) Find, in terms of n , an expression for the n th term of this sequence.

$$\begin{array}{ccccc} 5 & 11 & 17 & 23 & \\ 6n & 6 & 12 & 18 & 24 \end{array} \quad \dots \quad \dots$$

$6n - 1$
(2)

5. A sequence of numbers is shown.

$$2 \quad 9 \quad 16 \quad 23 \quad 30 \quad \dots \quad \dots$$

(a) Find an expression for the n th term of the sequence.

$$\begin{array}{cccc} 2 & 9 & 16 & 23 \\ 7 & 14 & 21 & 28 \end{array}$$

$$\begin{array}{c} 7n - 5 \\ \hline (2) \end{array}$$

(b) Find the 100th term in the sequence.

$$7 \times 100 - 5$$

$$\begin{array}{c} 695 \\ \hline (2) \end{array}$$

6. Here is the linear sequence

$$\begin{array}{cccc} 10 & 16 & 22 & 28 \\ b_n & 6 & 12 & 18 & 24 \end{array}$$

Circle the n th term of the sequence

$$4n + 6$$

$$n + 6$$

$$6n + 4$$

$$6n$$

(2)

7. The n th term of a number sequence is $n^2 + 3$

(a) Find the first three terms of this sequence.

1st term 4 , 2nd term 7 , 3rd term 12
(2)

(b) Work out the difference between the 5th and 10th terms in the sequence.

$\overbrace{5^2 + 3}^{5^{\text{th}} \text{ term}}$ $\overbrace{10^2 + 3 = 103}^{10^{\text{th}} \text{ term}}$

$103 - 28 = 75$ 75
(3)

8. The first 5 terms in a number sequence are

$-3n$ 10 7 4 1 -2

(a) Work out the n th term of the sequence.

$13 - 3n$

or

$-3n + 13$
(2)

(b) Find the 50th term of the sequence.

$13 - 3 \times 50$
 $13 - 150 = -137$
-137
(2)

9. Work out the n th term for this sequence

12 22 32 42 52
10_n 10 20 30 40 ...

$$\frac{10n+2}{(2)}$$

10. The n th term of a sequence is $3n - 2$

(a) Write down the first two terms of this sequence.

1st term 1 , 2nd term 4
(2)

(b) Which term of the sequence is equal to 70?

$$\begin{aligned}3n - 2 &= 70 \\3n &= 72 \\n &= 24\end{aligned}$$

24th
(2)

(c) Explain why 101 is not a term in the sequence.

$$\begin{aligned}3n - 2 &= 101 \\3n &= 103 \\n &= 34.333\ldots\end{aligned}$$

101 will be between the 34th and 35th terms in the sequence.

(2)

11. Here are the n th terms of 4 sequences.

Sequence 1	nth term	$3n + 1$
Sequence 2	nth term	$5n + 10$
Sequence 3	nth term	$10n$
Sequence 4	nth term	$5n - 1$

For each sequence state whether the numbers in the sequence are

- A Always multiples of 5
- S Sometimes multiples of 5
- N Never multiples of 5

$$3n + 1 \quad 4 \quad 7 \quad 10 \quad 13 \quad 16$$

$$5n + 10 \quad 15 \quad 20 \quad 25 \quad 30 \quad 35$$

$$10n \quad 10 \quad 20 \quad 30 \quad 40 \quad 50$$

$$5n - 1 \quad 4 \quad 9 \quad 14 \quad 19 \quad 24$$

Sequence 1 S

Sequence 2 A

Sequence 3 A
N

Sequence 4

(4)

12. The first four terms of an arithmetic sequence are

-25 -37 -49 -61

Find an expression, in terms of n , for the n th term of the sequence.

$$\begin{array}{cccc} -25 & -37 & -49 & -61 \\ -12n & -12 & -24 & -36 & -48 \end{array}$$

$$\begin{array}{r} -12n - 13 \\ \hline (2) \end{array}$$

13. The n th term of a sequence is $5 - 3n$

Write down the first three terms of the sequence.

$$\begin{array}{l} 5 - 3 \times 1 \\ 5 - 3 = 2 \end{array}$$

$$\begin{array}{l} 5 - 3 \times 2 \\ 5 - 6 = -1 \end{array}$$

$$\begin{array}{l} 5 - 3 \times 3 \\ 5 - 9 = -4 \end{array}$$

$$\begin{array}{l} 2 \\ 1st \text{ term} \dots, 2nd \text{ term} \dots, 3rd \text{ term} \dots \\ (2) \end{array}$$

14. The n th term of a sequence is $4n - 7$

(a) Write down the first three terms of the sequence.

1st term -3, 2nd term 1, 3rd term 5
(2)

(b) What is the difference between the 150th and 151st terms?

4

..... 4
(1)

The last term of this sequence is 393

(c) How many terms are there in this sequence?

$$\begin{aligned}4n - 7 &= 393 \\+7 &+7 \\4n &= 400 \\n &= 100\end{aligned}$$

..... 100
(2)

15. Find the nth term of the sequences

(a) 1, 4, 9, 16, 25, ...

$$\dots n^2 \dots$$

(1)

(b) 3, 6, 11, 18, 27, ...

$$\dots n^2 + 2 \dots$$

(1)

(c) -3, 0, 5, 12, 21, ...

$$\dots n^2 - 4 \dots$$

(1)

(d) 2, 8, 18, 32, 50, ...

$$\dots 2n^2 \dots$$

(1)

16. The nth term of a sequence is $9n + 7$

Write down all the numbers from the sequence that are **prime** and **less than 100**.

16 25 34 $\textcircled{43}$ 52 $\textcircled{61}$ 70 $\textcircled{79}$ 88
 $\textcircled{97}$

....., 43, 61, 79, 97,

.....
(2)

17. The first 5 terms in a number sequence are

30 25 20 15 10

Work out the n th term of the sequence.

$-15n$ -5 -10 -15 -20

$35 - 5n$

or

$-5n + 35$

(2)

18. Here are the first four terms of an arithmetic sequence

9 17 25 33

(a) Find an expression, in terms of n , for the n th term of the sequence

9 17 25 33
 s_n 8 16 24 32

$s_n + 1$

(2)

The n th term of a difference sequence is $20 - 3n$

(b) Is -71 a term in the sequence?

Show your working out.

$$20 - 3n = -71$$

$$20 = -71 + 3n$$

$$91 = 3n$$

$$n = 30.333 \dots$$

No

(2)

19. The first 5 terms in a number sequence are

$$0.5n + 1.5 \quad 2.5 \quad 2.5 \quad 3 \quad 3.5 \quad 4 \quad \dots \quad \dots$$

(a) Work out the n th term of the sequence.

$$\begin{array}{r} 0.5n + 1.5 \\ \hline \end{array} \quad (2)$$

(b) Work out the 20th term of the sequence.

$$\begin{array}{r} 0.5 \times 20 + 1.5 \\ 10 + 1.5 \\ \hline 11.5 \end{array} \quad (2)$$

20. The 4th term of a linear sequence is 26
The 6th terms of the same sequence is 32

Work out the n th term of the sequence.

$$\begin{array}{cccccc} 17 & 20 & 23 & 26 & 29 & 32 \\ 3n & 3 & 6 & 9 & 12 & \end{array}$$

$$\begin{array}{r} 3n + 14 \\ \hline \end{array} \quad (3)$$

21. The first 5 terms of a sequence are

$$\begin{array}{cccccc} & 1 & 5 & 9 & 13 & 17 \\ 4n & 4 & 8 & 12 & & \end{array}$$

(a) Work out the n th term for this sequence.

$$\frac{4n-3}{11n+1} \quad (2)$$

The first 5 terms of a sequence are

$$\frac{1}{12} \quad \frac{5}{23} \quad \frac{9}{34} \quad \frac{13}{45} \quad \frac{17}{56}$$

(a) Work out the n th term for this sequence.

$$\begin{array}{cccccc} 12 & 23 & 34 & 45 & \dots \\ 1n & 11 & 22 & 33 & 44 \\ & & 11n+1 & & & \end{array} \quad \frac{4n-3}{11n+1} \quad (2)$$

22. Here are the first 4 terms of a sequence

$$\frac{2}{3} \quad \frac{3}{5} \quad \frac{4}{7} \quad \frac{5}{9} \quad \frac{6}{11}$$

(a) Find the next term of the sequence

$$\frac{6}{11} \quad (1)$$

(b) Find the n th term of the sequence

$$\begin{array}{cccccc} 2 & 3 & 4 & 5 & & \\ n & 1 & 2 & 3 & 4 & \\ & \underline{n+1} & & & & \end{array} \quad \begin{array}{cccccc} 35 & 7 & 9 & & & \\ n & 2 & 4 & 6 & 8 & \\ & \underline{2n+1} & & & & \end{array} \quad \frac{n+1}{2n+1} \quad (1)$$

23. Here are the first 4 terms of a sequence

$$\frac{7}{8} \quad \frac{9}{11} \quad \frac{11}{14} \quad \frac{13}{17}$$

Write down the 20th term of the sequence.

7 $2n$	9 2	11 4	13 6	$3n$	8 3	11 6	14 9	17 12	
					$3n+5$				
				$2n+5$					
				$\frac{2n+5}{3n+5}$	$\frac{45}{65}$			$\frac{9}{13}$	

24. Martin has written the first 50 terms of the sequence with n th term $150 - 4n$.

Work out which term is the first negative term.

Approach 1

$$150 - 4 \times 30 = 30$$

$$150 - 4 \times 35 = 10$$

$$150 - 4 \times 37 = -2$$

$$150 - 4 \times 38 = -2$$

Approach 2

$$150 - 4n = 0$$

$$150 = 4n$$

$$n = 37.5$$

38th

..... 38th term (-2)
(3)

25. The first 4 terms of sequence A are

$$5n \quad 4 \quad 9 \quad 14 \quad 19$$

(a) Find the n th term of sequence A.

$$5n - 1$$

(2)

The n th term of sequence B is $2n + 6$

The n th terms of sequence A and sequence B are added together to give the n th term of sequence C.

Is 1000 a term in sequence C?

$$\begin{array}{r} 5n - 1 \\ 2n + 6 \\ \hline 7n + 5 \end{array} \quad \begin{array}{l} 7n + 5 = 1000 \\ 7n = 995 \\ n = 142.142\ldots \end{array}$$

No

(2)

26. The n th term of a sequence is $(n + 1)(n + 3)$

Work out the first three terms of the sequence.

$$1^{\text{st}} \text{ term} \quad 2 \times 4 = 8$$

$$2^{\text{nd}} \text{ term} \quad 3 \times 5 = 15$$

$$3^{\text{rd}} \text{ term} \quad 4 \times 6 = 24$$

$$\begin{array}{l} 6 \quad 15 \quad 24 \\ \text{1st term} \dots, \text{2nd term} \dots, \text{3rd term} \dots \\ (2) \end{array}$$